

3a) i) $(\lambda x y \rightarrow x + 2 * y) (2 * 6) (3 * 8)$
evaluiert laut ghci zu 60 ✓ $\frac{3}{3}$

ii) $(\lambda f g h \rightarrow f(g(x)) (g(x)))$

$(\lambda x y \rightarrow x + 2 * y)$

$((\lambda x y z \rightarrow ((\lambda x y \rightarrow x + 2 * z) x z)$

$- ((\lambda x y \rightarrow x + 2 * y) (2 * x) y))$

1 2) 3

evaluiert laut ghci zu 3 ✓ $\frac{5}{5}$

iii) $(\lambda x y \rightarrow x + 2 * y)$

$((\lambda x y z \rightarrow ((\lambda a b \rightarrow a + 2 * b) x z)$

$- ((\lambda a b \rightarrow a + 2 * b) (2 * x) y))$ 123)

$((\lambda x y \rightarrow x + 2 * y) 2 * 7)$

evaluiert laut ghci zu 33 ✓ $\frac{5}{5}$

b) Wenn man Data.Funktion importiert, ist es problemlos möglich die Collatz-Funktion mit Lambda ausdrücken auszu drücken:

import Data.Funktion

fix $(\lambda c n \rightarrow \text{if } n == 1 \text{ then } [1]$

else if even n then n : c (n `div` 2)

else n : c (3 * n + 1)) 5

evaluiert zu [5, 16, 8, 4, 2, 1] laut ghci

Andernfalls, ohne den der Fixpunktoperation, würde sich

der Aufruf der Lambda-Funktion für jede Rekursion

vergrößern, mit stets anderen Werten für n.

Sollte die Collatzfunktion für eine Eingabe nicht terminieren,

so wäre der Funktionsaufruf unendlich lang. Das geht nicht!

✓ $\frac{2}{2}$

1a) $s := (\lambda x. \lambda y. \lambda z. ((x\ y)\ z)) (\lambda x. \lambda y. (x\ (\lambda y. \lambda z. z)))$

b) $(\lambda x y z \rightarrow x y z) (\lambda x y \rightarrow x) (\lambda y z \rightarrow z)$ Ausgabe? $\frac{2}{5}$

c) Alle Variablen sind gebunden.

$\Rightarrow (\lambda abc \rightarrow abc) (\lambda de \rightarrow d) (\lambda fg \rightarrow g)$ $\frac{5}{5}$

a) $s := (\lambda x. \lambda y. \lambda z. ((x\ y)\ z)) (\lambda x. \lambda y. (x\ (\lambda y. (\lambda z. z))))$

b) $(\lambda x y z \rightarrow x y z) (\lambda x y \rightarrow x) (\lambda y z \rightarrow z)$

No instance Show $((t_2 \rightarrow t_3 \rightarrow t_3) \rightarrow t_0) \rightarrow t_1 \rightarrow t_0$

2) collatz 1 = trace "1" 1

collatz n = trace Show \$n if even n then collatz (n `div` 2)
else collatz (3*n + 1)

Haskell Code:

```
"  
import System.IO  
import Data.Char
```

← braucht man wirklich System.IO ?

```
main = do
```

```
writeFile "01.txt" (show $ collatz $ 2^33)  
writeFile "02.txt" (show $ collatz $ 235)  
writeFile "03.txt" (show $ collatz $ 5)  
writeFile "04.txt" (show $ collatz $ 82654)  
writeFile "05.txt" (show $ collatz $ 1337)  
writeFile "06.txt" (show $ collatz $ 420)  
writeFile "07.txt" (show $ collatz $ 69)  
writeFile "08.txt" (show $ collatz $ 66)  
writeFile "09.txt" (show $ collatz $ 42)  
writeFile "10.txt" (show $ collatz $ 31415926)
```

Die Idee ist richtig
trotzdem solltest du, wenn
du vorhatst in
Haskell zu
programmieren
"trace" lernen

```
collatz :: Integer -> [Integer]  
collatz a = if a == 1 then [1] else  
  if even a then a : collatz (a `div` 2)  
  else a : collatz ((3*a)+1)
```

20/20

Erzeugt Ausgaben

01.txt

```
[8589934592,4294967296,2147483648,1073741824,536870912,268435456,1342177  
28,67108864,33554432,16777216,8388608,4194304,2097152,1048576,524288,2621  
44,131072,65536,32768,16384,8192,4096,2048,1024,512,256,128,64,32,16,8,4,2,1]
```

02.txt

```
[235,706,353,1060,530,265,796,398,199,598,299,898,449,1348,674,337,1012,506,25  
3,760,380,190,95,286,143,430,215,646,323,970,485,1456,728,364,182,91,274,137,4  
12,206,103,310,155,466,233,700,350,175,526,263,790,395,1186,593,1780,890,445,1  
336,668,334,167,502,251,754,377,1132,566,283,850,425,1276,638,319,958,479,143  
8,719,2158,1079,3238,1619,4858,2429,7288,3644,1822,911,2734,1367,4102,2051,6  
154,3077,9232,4616,2308,1154,577,1732,866,433,1300,650,325,976,488,244,122,61  
,184,92,46,23,70,35,106,53,160,80,40,20,10,5,16,8,4,2,1]
```

03.txt

```
[5,16,8,4,2,1]
```

04.txt

```
[82654,41327,123982,61991,185974,92987,278962,139481,418444,209222,104611,  
313834,156917,470752,235376,117688,58844,29422,14711,44134,22067,66202,331
```

01,99304,49652,24826,12413,37240,18620,9310,4655,13966,6983,20950,10475,314
26,15713,47140,23570,11785,35356,17678,8839,26518,13259,39778,19889,59668,2
9834,14917,44752,22376,11188,5594,2797,8392,4196,2098,1049,3148,1574,787,23
62,1181,3544,1772,886,443,1330,665,1996,998,499,1498,749,2248,1124,562,281,84
4,422,211,634,317,952,476,238,119,358,179,538,269,808,404,202,101,304,152,76,3
8,19,58,29,88,44,22,11,34,17,52,26,13,40,20,10,5,16,8,4,2,1]

05.txt

[1337,4012,2006,1003,3010,1505,4516,2258,1129,3388,1694,847,2542,1271,3814,1
907,5722,2861,8584,4292,2146,1073,3220,1610,805,2416,1208,604,302,151,454,22
7,682,341,1024,512,256,128,64,32,16,8,4,2,1]

06.txt

[420,210,105,316,158,79,238,119,358,179,538,269,808,404,202,101,304,152,76,38,1
9,58,29,88,44,22,11,34,17,52,26,13,40,20,10,5,16,8,4,2,1]

07.txt

[69,208,104,52,26,13,40,20,10,5,16,8,4,2,1]

08.txt

[66,33,100,50,25,76,38,19,58,29,88,44,22,11,34,17,52,26,13,40,20,10,5,16,8,4,2,1]

09.txt

[42,21,64,32,16,8,4,2,1]

10.txt

[31415926,15707963,47123890,23561945,70685836,35342918,17671459,53014378,
26507189,79521568,39760784,19880392,9940196,4970098,2485049,7455148,3727
574,1863787,5591362,2795681,8387044,4193522,2096761,6290284,3145142,15725
71,4717714,2358857,7076572,3538286,1769143,5307430,2653715,7961146,398057
3,11941720,5970860,2985430,1492715,4478146,2239073,6717220,3358610,167930
5,5037916,2518958,1259479,3778438,1889219,5667658,2833829,8501488,4250744
,2125372,1062686,531343,1594030,797015,2391046,1195523,3586570,1793285,53
79856,2689928,1344964,672482,336241,1008724,504362,252181,756544,378272,1
89136,94568,47284,23642,11821,35464,17732,8866,4433,13300,6650,3325,9976,49
88,2494,1247,3742,1871,5614,2807,8422,4211,12634,6317,18952,9476,4738,2369,7
108,3554,1777,5332,2666,1333,4000,2000,1000,500,250,125,376,188,94,47,142,71,
214,107,322,161,484,242,121,364,182,91,274,137,412,206,103,310,155,466,233,700
,350,175,526,263,790,395,1186,593,1780,890,445,1336,668,334,167,502,251,754,37
7,1132,566,283,850,425,1276,638,319,958,479,1438,719,2158,1079,3238,1619,4858
,2429,7288,3644,1822,911,2734,1367,4102,2051,6154,3077,9232,4616,2308,1154,5
77,1732,866,433,1300,650,325,976,488,244,122,61,184,92,46,23,70,35,106,53,160,8
0,40,20,10,5,16,8,4,2,1]